

## Hemingbrough CP School

### **Maths Calculation Policy Guidance**

Written methods of calculation for Addition.

Step 1	
Step 1Concrete additionThis step requires the children to combine two groups of objects or images. Eg. Count out 3, add two more. How many do we have now?Use of fingers is encouraged as this is a constantly available resource.The number sentence should be related to	For example: $3 + 2 = 5$ For example For example 5 + 1 = 6
The number sentence should be related to the objects/pictures/fingers whenever possible. Eg. 3 teddies + 2 teddies = 5 teddies Children need to be able to verbalise calculations in 'everyday language' before introducing symbols e.g. 'I had 3 teddies and you gave me 2 more. Now I've got 5' When discussing problems, this should also be introduced as a <b>bar model</b> , initially drawn round the objects and then blank.	$\begin{array}{c} & & & \\ & & & \\ & & & \\ \hline \end{array} \\ \hline $
Step 2	

Counting on	For example: 5 + 4 = 9
This step requires the children to realise that there is no need to count from the start each time. They combine a hidden number with a concrete number ie. The first number in their head, the second on their fingers, or 6 cakes already in a box, if I add 2 more, how many do I have now? They should be encouraged to discover that it is easier to put the biggest number in their heads.	$ \begin{array}{c}                                     $
This is to be recorded on a <b>numbered number line</b> .	8 + 5 = 13 
When discussing problems, this should also be introduced with the use of a <b>bar model</b> as above.	3+4=7
Step 3	
Empty number line	For example:
	48 + 36 = 84
This step requires the children to record addition on a blank number line.	+30 +30 +2 +2 +2 +4 80 84 08 +2 +34
The steps should be extended so that they bridge through a multiple of ten.	48 50 84
Additions should involve single digit numbers as well as two and three digit numbers. The method can also be used for adding decimals.	//፡፡ ////፡:
Children should be encouraged to use their knowledge of number bonds here e.g. if I'm adding 17 + 8 and I know the pairs that make 8 and I know what to add to 17 to get to the next ten, I would probably think of 17 + 8 as 17 + 3 + 5	25 + 47 = 72
	,
	32 25

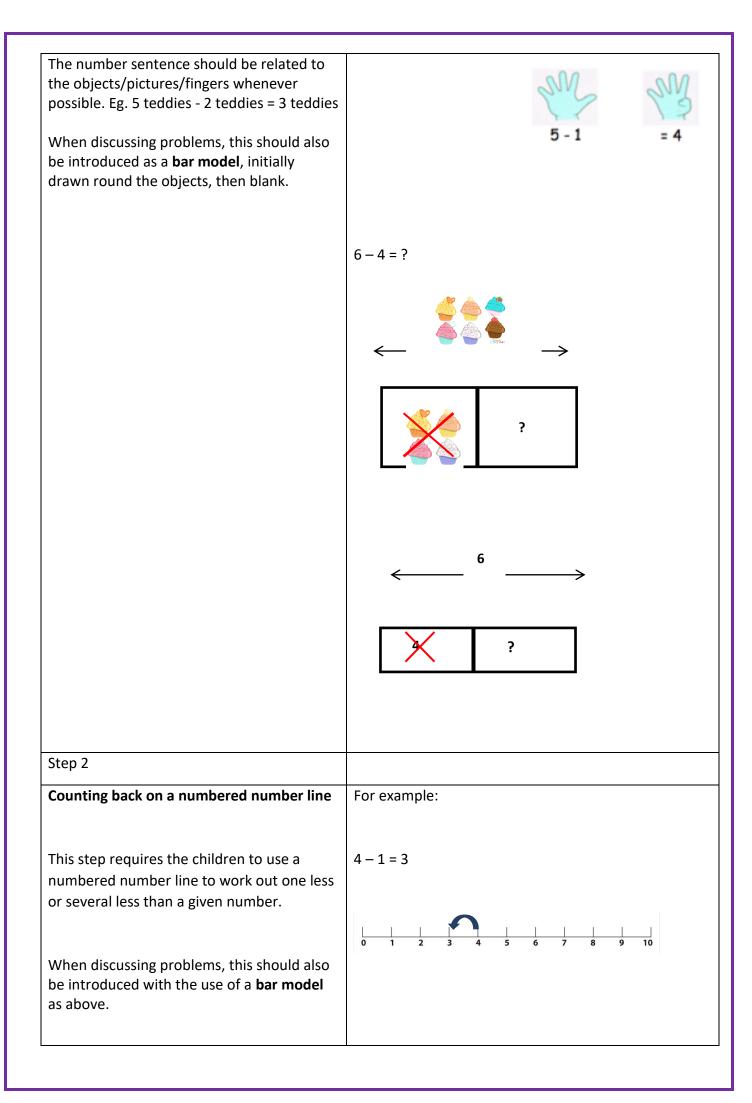
Use of straws, Base 10 or Place Value counters should be used to reinforce the value of each digit.	32 + 25 = 57
Problem solving should include the use of <b>bar modelling</b> to aid visualisation.	45 + ? = 79 <u>~~</u> 79 <u>~</u>
Step 4	45 ?
Partitioning	For example:
This step requires the children to partition the number, add these partitions and then add the partial sums.	47 + 76
	40 + 70 = 110
	7 + 6 = 13
This method can be used for 3 digit numbers and decimals.	110 + 13 - 123
Use of straws, Base 10 or Place Value counters should be used to reinforce the value of each digit.	324 + 241
	300 + 200 = 500
Problem solving should include the use of <b>bar</b> <b>modelling</b> to aid visualisation as above.	20 + 40 = 60
	4 + 1 = 5
	500 + 60 + 5 = 561
	45.3 + 56 .8
	40 + 50 = 90
	5 + 6 = 11
	.3 + .8 = 1.1
	90 + 11 + 1.1 = 102.1

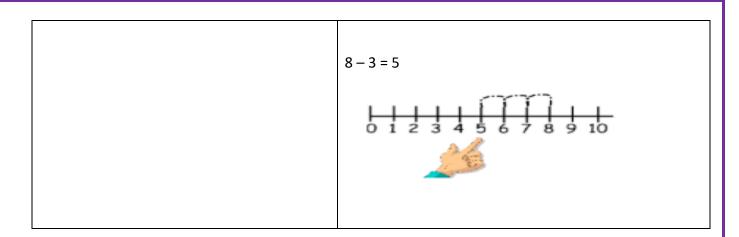
Step 5	
<b>Extended column</b> This step requires the children to set the calculation out in a column (being careful to ensure correct place value). They are then required to add the <b>lowest value digit first</b> ,	For example: $+\frac{83}{-42}$ $\frac{120}{125}$ 367 14.28 14.28 147.56
recording the answer below before moving to the other digits and adding the partial sums.	$\begin{array}{c cccc} +185 & +17.56 \\ \hline 12 & 0.14 \\ 140 & 0.70 \\ \underline{400} & 11.00 \\ 552 & \underline{20.00} \\ 31.84 \end{array}$
This method can be used when adding 2, 3 or 4 digit numbers as well as decimals.	
Use of straws, Base 10 or Place Value counters should be used to reinforce the value of each digit.	
These should be placed onto a grid clearly	Example using straws on a calculation mat:
marked with Hundreds, Tens, Units (as appropriate)	⊡         Calculation mat           100's         10's
Problem solving should continue to include	
Problem solving should continue to include the use of <b>bar modelling</b> to aid visualisation as in previous steps.	Bring the ground row to and the boltom row to add
the use of <b>bar modelling</b> to aid visualisation	Binnative source for vio

Short method	
	For example:
This method requires the children to set the calculation out in a column (being careful to ensure correct place value).	367 <u>+185</u> <u>552</u> 1 1
When adding, the children are required to <b>begin with the units</b> , and carry using correct language such as 'carry ten' or 'carry one hundred'. The number carried should be recorded <b>below</b> the line.	3587 + <u>675</u> <u>4262</u> 1 1 1
This method should be extended to addition of 3, 4 and 5 digit numbers as well as decimals, and can be extended to adding more than two numbers.	72.8 +54.6 127.4 1 1 13.86 + 9.481
Use of straws, Base 10 or Place Value counters can continue to be used to reinforce the value of each digit. Placed onto a grid clearly marked as appropriate.	<u>23.341</u> 1 1 1
Problem solving should continue to include the use of <b>bar modelling</b> to aid visualisation as in previous steps.	

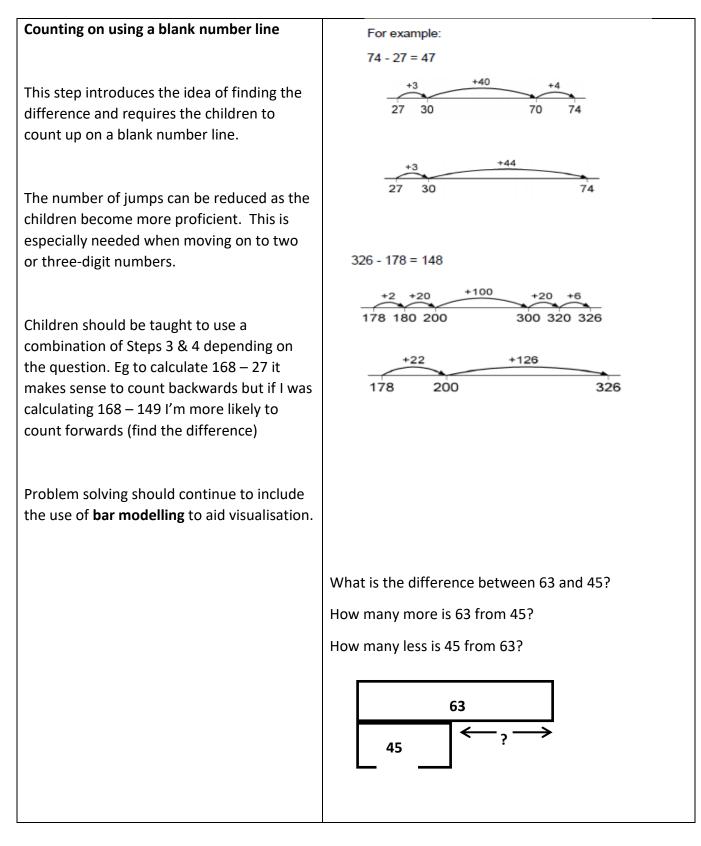
#### Written methods of calculation for Subtraction.

Step 1	
Concrete subtraction	For example:
This step requires the children to physically take away one or more objects from a set of objects.	
Children will also cross out images to take away.	5 – 2 = 3
Use of fingers is encouraged as this is a constantly available resource.	





Step 3	
Counting back on a blank number line	For example:
This step requires the children to count backwards using a blank number line.	$32 - 17 = 15$ $\underbrace{\begin{array}{c}15 \\ -5\end{array}}_{-5} \underbrace{\begin{array}{c}20 \\ -2\end{array}}_{-10} \underbrace{\begin{array}{c}32 \\ -10\end{array}}_{-10}$
The number of jumps can be reduced as the children become more proficient.	74 - 27 = 47 $-3 -4 -20$ $47 - 50 - 54 -74$
They should also be encouraged to use their understanding of the number system to speed up calculations eg. 74 - 27 might be usefully calculated as 74 – 30 + 3	63 – 45 = ?
Problem solving should include the use of <b>bar modelling</b> to aid visualisation.	63 45 ?
Step 4	



Step 5

#### Expanded column method

This step requires the children to partition the numbers and then subtract the **lowest** value digits first.

It should be used to introduce the idea of decomposition and **carrying**.

This method should be used for two and three-digit numbers and can be extended to decimals.

# Use of straws, Base 10 or Place Value counters should be used to reinforce the value of each digit.

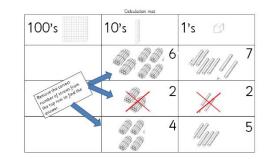
These should be placed onto a grid clearly marked with Hundreds, Tens, Units (as appropriate)

Problem solving should continue to include the use of **bar modelling** to aid visualisation as in previous steps. For example:

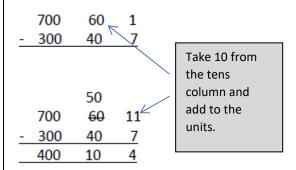
77 - 24 = 53

70	7
- 20	4
50	3

Using straws:

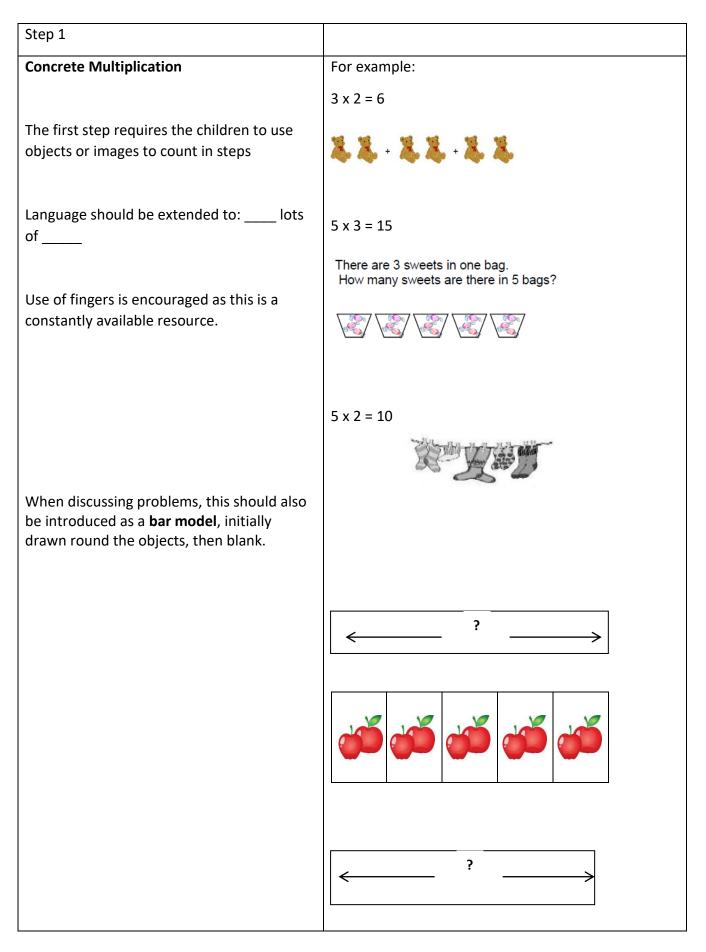






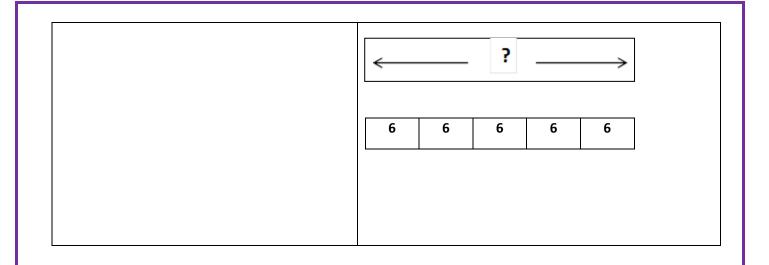
Step 6	
Short method (decomposition)	For example:
This step requires the children to set the calculation out in a column (being careful to	537 - 214 = 323 537 - 214
ensure correct place value).	<u>323</u> 728 - 51 = 677
They should subtract the right hand column (units) first and carry from the left hand side column if needed.	$\frac{6}{7}28}{-51}{-677}$
Use of straws, Base 10 or Place Value counters should be used to reinforce the value of each digit as before.	Use of place value counters when carrying:
This method can be used for any number of digits as well as decimals.	Column Subtraction with Place Value Counters
Problem solving should continue to include the use of <b>bar modelling</b> to aid visualisation as in previous steps.	400 590 160 90 6 300 + 70 + 3 = 373 ✓
	Written method:
	352 - 168 =
	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
	Stages of working shown

#### Written methods of calculation for Multiplication.



2	2	2	2	2	

Step 2				
Arrays	For example:			
This step requires the children to use objects or pictures in arrays.	$2 \times 3 = 6$ $3 \times 2 = 6$			
It should be extended to arrays of dots or circles.	3 x 4 = 12 4 x 3 = 12			
	3 x 6 = 18 6 x 3 = 18			
Step 3				
<b>Repeated addition on number line</b> This step requires the children to show repeated addition using number lines.	For example: $4 \times 3 = 12$ $\begin{array}{r} +3 & +3 & +3 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \end{array}$			
Counting in steps of should be practised at this point. Fingers can be used to keep track of how many lots of you have counted.	Counting in 5's: "5, 10, 15, 20"			
Problem solving should include the use of <b>bar modelling</b> to aid visualisation.	Problem solving: Pencils come in packs of 6. If I buy 5 packs, how many pencils do I have?			



Step 4	
Partitioning	
This step requires the children to use arrays to visualise the partitioning of larger numbers, then they can find the total of each section.	$13 \times 18 = 234$ $10$ $10$ $3$ $10$ $10$ $3$ $10$ $10$ $3$ $3$ $10$ $10$ $3$ $3$ $10$ $10$ $3$ $3$ $3$ $10$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$
This directly relates to the following step (Grid method).	
	100 + 80 + 30 + 24 = 234
	$10 \\ 100 \\ 3 \\ 3 \\ 3 \\ 3 \\ 24 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $
Step 5	
Grid Method	For example:
This step requires the children to place their partitioned numbers into a grid. They multiply each part of the number before adding the partial results.	$123 \times 5 = 615$ $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
This method should be used for multiplication by one and two digit numbers and can be extended to include decimals.	+ 15 615

	$56 \times 2.3 = 128.8$ $\times 50 6$ $2 100 12$ $0.3 15 1.8$	100.0 12.0 15.0 1.8 128.8
	815 x 34 = <b>x</b> 800 10 5 30 24000 300 150 4 3200 40 20	24000 300 150 3200 40 <u>20</u> 27710
Step 6		
Extended column method	For example:	
This step requires the children to set the calculation out on in column and then multiply each partition together <b>(units, then tens, then hundreds)</b> before adding the partial calculation together.	38 x 7 = 266 HTU 38 <u>x 7</u> 56 210 266	$\begin{array}{c} 32 \\ x \underline{24} \\ 8 \\ 120 \\ 40 \\ 20 \\ x 2) \\ \underline{600} \\ 768 \end{array}$ $(4 \times 2) \\ (4 \times 30) \\ (20 \times 2) \\ \underline{600} \\ 768 \end{array}$
This method should be extended to multiplication by two and three digit numbers, and multiplication of decimals. Children should describe what they do by referring to the actual values of the digits in the columns. For example, in 38 × 7 is 'thirty multiplied by seven', or 'three tens times 7 units', not 'three times seven', although the relationship to 3 × 7 should be stressed.	286 x 29 = 8294 THTU 286 x 29 54 720 1800 120 1600 <u>4000</u> <u>8294</u>	
Step 7		

Short Method for x U	For example:	
	38 x 7 = 266	934 x 6 = 5604
This step requires the children to use carrying to shorten the method. This method can be used effectively for multiplication of decimals. The carried number should be placed underneath the appropriate column	HTU 38 <u>X 7</u> <u>266</u> 237 x 4 = 948	Th H T U 9 3 4 6 5 6 0 4 2 2
	$x \frac{237}{948}_{12}$	

Step 8	
Step 8 Short Method for x TU This method requires the children to multiply the larger number by the units and then the larger number by the tens, and so on, before adding the two numbers together. Carried numbers should once again be placed underneath the appropriate column	For example: Multiply the units first and carry any tens across: $3 \times 8 = 24$ (carry the 2 tens) Then multiply the units by the tens, add the carried digit, then carry again: $3 \times 5 = 15 + 2 = 17$ (carry the 1) Multiply the units by the hundreds, add the carried digit: $3 \times 9 = 27 + 1 = 28$

#### Written methods of calculation for Division.

Step 1	
Concrete Sharing	For example:
	6 ÷ 2 = 3 (six shared by 2)
The first step requires the children to use objects or images to share.	XX XX
Language should be extended to: shared by	21 ÷ 3 = 7
The division number sentence should be shown alongside the calculations.	
Remainders are expressed as 1 left, 2 left etc.	15 ÷ 5 = 3
	I have 10 sweets, if I share them between 5 people, how many do they get each?
When discussing problems, this should also be introduced as a <b>bar model</b> , initially drawn round the objects, then blank.	
	? ? ? ? ? 
Step 2	

#### **Concrete Grouping**

The children should recognise division as grouping as well as sharing. This can be done with objects or images.

Language should be extended to : How many groups of \_\_\_\_\_ can we get out of \_\_\_\_\_?

The division number sentence should be shown alongside the calculations.

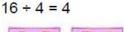
Remainders are expressed as 1 left, 2 left There is also a need in some problems which leave a remainder to round up or down. Eg. How many bags do I need / how many full bags have I got, etc

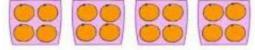
When discussing problems, this should also be introduced as a **bar model** as above.

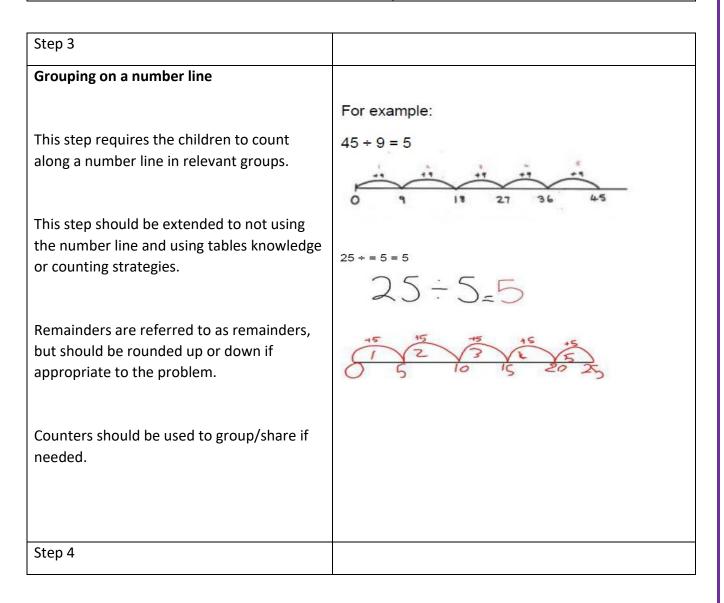
#### For example:

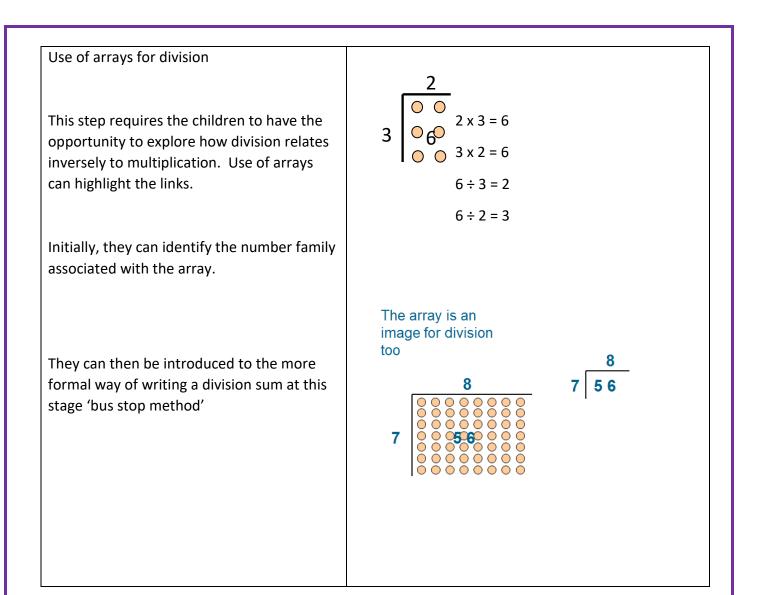
 $12 \div 4 = 3$  (How many groups of 4 are there in 12?











Step 5	
Place Value Counters	For example:
This step requires the children to divide larger value digits using place value counters. The method should be used to divide TU and HTU by U	$364 \div 3 = $ $121 r 1$ $3 3 6 4$ National Centre Versions of Mathematics
Begin by dividing the <b>largest digit first</b> (eg hundreds, tens, then units)	
The dialogue going on in the learner's head, e.g. for 364 ÷ 3 I would ask myself 'How many groups of 3-hundreds can I make from the hundreds; how many groups of 3-tens can I make from the tens, etc	Questions requiring carrying/exchanging:
The method should be extended to questions that require carrying.	345÷3= 3 345
The method should be used <b>alongside step</b> <b>6</b> to ensuring understanding of both.	
Remainders should be rounded up or down if appropriate to the problem.	Here, we need to carry / exchange one of the tens for 10 ones:

	1 1 5 3 3 4 <sup>1</sup> 5	Teaching of Mathematics 🥣	
(0) (0) (0)	•		

Step 6	
Short method for ÷ U ('Bus stop method')	For example:
This step requires the children to <b>carry</b> remainders within the calculation to make it more efficient. It should be used to divide TU, HTU, ThHTU as well as decimals. The method should initially be taught <b>alongside step 5</b> so the children understand	964 ÷ 7 = 137 r5 or 137 5/7 <b>1 3 7 r 5</b> <b>7 9<sup>2</sup>6<sup>5</sup>4</b>
what they are carrying and why.	847 ÷ 5 = 169r2 or 169 2/5
Decimal places should be added to show remainders as decimals.	5 847
When problem solving, remainders should be rounded up or down if appropriate. Children can also be taught how to express remainders as fractions.	79 ÷ 5 = 15.8
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Step 7	
Short method for ÷ TU	
	For example:
This step requires the children to divide by TU. It requires the same method as step 5 although the children should be encouraged to write the tables of the divisor.	869 ÷ 32 = 27 r5 64 96 128
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$

#### Step 3: A remainder in the tens

In this step, students practice for the first time all the basic steps of long division algorithm: divide, multiply & subtract, drop down the next digit. We use two-digit numbers to keep it simple. Multiply & subtract has to do with finding the *remainder*, and after finding a remainder, we combine that with the next unit we are getting ready to divide (dropping down the digit).

#### An example:

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o <mark>2</mark> 2 ) <mark>5</mark> 8	t o 2 2 ) <u>5</u> 8 <u>-4</u> 1	t o 2 9 2 ) 5 8 -4 1 1 8
Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens but there is a remainder!	To find it, multiply $2 \times 2 = 4$ , write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o	t o	t o
29	29	29
2)58 -4	2)58	2)58
18	18	18
	<u>- 18</u> 0	<u>- 1 8</u> 0
Divide 2 into 18. Place 9 into the quotient.	Multiply $9 \times 2 = 18$ , write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.

#### Step 4: A remainder in any of the place values

After the previous step has been mastered, students then practice long division with three- and four-digit numbers where they will have to go through the basic steps several times.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
hto <mark>1</mark> 2)278	h t o 1 2) <mark>2</mark> 7 8 -2 0	$ \begin{array}{r} h \ t \ o \\ 1 \ 8 \\ 2 \ \hline 2 \ 7 \ 8 \\ - 2 \\ \hline 0 \ 7 \end{array} $
Two goes into 2 one time, or 2 hundreds ÷ 2 = 1 hundred.	Multiply $1 \times 2 = 2$ , write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
$     \begin{array}{r}             h t o \\             1 3 \\             2) 2 7 8 \\             -2 \\             -2 \\           $		$ \begin{array}{r}             h t o \\             1 3 \\             2 ) 2 7 8 \\             -2 \\             -2 \\           $
Divide 2 into 7. Place 3 into the quotient.	Multiply 3 × 2 = 6, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
h t o <u>1 3 9</u> <u>2 ) 2 7 8</u> <u>- 2</u> 0 7 <u>- 6</u> <u>1 8</u>	h t o <u>1 3 9</u> 2 ) 2 7 8 <u>-2</u> 0 7 <u>- 6</u> <u>1 8</u> <u>- 1 8</u> 0	h t o 139 2)278 -2 07 -6 18 -18 0
Divide 2 into 18. Place 9 into the quotient.	Multiply $9 \times 2 = 18$ , write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.

#### Notes for all calculations:

It is vitally important that children begin to use known facts and derive new facts from these as soon as possible.

Eg.

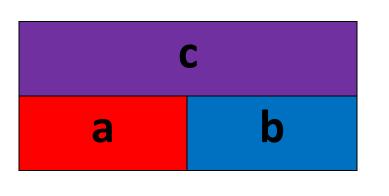
If I know that 2 + 3 = 5, then I also know that 3 + 2 = 5.

From this I can work out that 5 - 3 = 2 and 5 - 2 = 3.

I can also see that 20 + 30 = 50, 30 + 20 = 50, 50 - 30 = 20 & 50 - 20 = 30

Children need to understand the relationship between operations.

Eg. subtraction is the opposite of addition, and division is the opposite of multiplication.



This bar model shows the relationship between addition and subtraction.
a + b = c
b + a = c
c – a = b
c – b = a

р				
n	n	n	n	n

This bar model shows the
relationship between
multiplication and division.

5 x n = p

Date of Policy Adoption / Reviewed	Responsibility / Reviewed by	Revisions Made (Y/N)	Method of Communication	Date of Next Review
Jul 2021	FGB	N	Website	Jul 2024