Hemingbrough Primary School Calculation Framework – Working Document Updated 01/09/2022

Mathematics Mastery

At the centre of the mastery approach to the teaching of mathematics is the belief that **all children have the potential to succeed**. They should have access to the same curriculum content and, rather than being extended with new learning, they should **deepen their conceptual understanding by tackling challenging and varied problems**. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in Year 1 to Year 6 in line with the requirements of the 2014 Primary National Curriculum.

Background

The 2014 Primary National Curriculum for mathematics differs from its predecessor in many ways. Alongside the end of Key Stage year expectations, there are suggested goals for each year; there is also an emphasis on depth before breadth and a greater expectation of what children should achieve. In addition, there is a whole new assessment method, as the removal of levels gives schools greater freedom to develop and use their own systems. One of the key differences is the level of detail included, indicating what children should be learning and when. This is suggested content for each year group, but schools have been given autonomy to introduce content earlier or later, with the expectation that by the end of each key stage the required content has been covered. For example, in Year 2, it is suggested that children should be able to 'add and subtract one-digit and two-digit numbers to 20, including zero' and a few years later, in Year 5, they should be able to 'add and subtract whole numbers with more than four digits, including using formal written methods (columnar addition and subtraction)'. In many ways, these specific objectives make it easier for teachers to plan a coherent approach to the development of pupils' calculation skills. However, the expectation of using formal methods is rightly coupled with the explicit requirement for children to use concrete materials and create pictorial representations – a key component of the mastery approach.

Mathematical Language

The 2014 National Curriculum is explicit in articulating the importance of children using the correct mathematical language as a central part of their learning (*reasoning*). Indeed, in certain year groups, the non-statutory guidance highlights the requirement for children to extend their language around certain concepts. It is therefore essential that teaching using the strategies outlined in this policy is accompanied by the use of appropriate and precise mathematical vocabulary. New vocabulary should be introduced in a suitable context (for example, with relevant real objects, apparatus, pictures or diagrams) and explained carefully. High expectations of the mathematical language used are essential, with teachers only accepting what is correct. The school agreed list of terminology is located at Appendix A to this document.

How to use the framework

This mathematics framework is a guide for all staff at Hemingbrough Primary school and has been adapted from work by the NCETM. It is purposely set out as a progression of mathematical skills and not into year group phases to encourage a flexible approach to teaching and learning. It is expected that teachers will use their professional judgement as to when consolidation of existing skills is required or if to move onto the next concept. However, the **focus must always remain on breadth and depth rather than accelerating through concepts.** Children should not be extended with new learning before they are ready, they should deepen their conceptual understanding by tackling challenging and varied problems. All teachers have been given the scheme of work from NCETM and White Rose Maths and are required to base their planning around their year groups modules and not to move onto a higher year groups scheme work.

Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used. For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Make it, Draw it, Write it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.

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The quality and variety of language that pupils hear and speak are key factors in developing their mathematical vocabulary and presenting a mathematical justification, argument or proof.

2014 Maths Programme of Study

Content of the Policy

For ease of movement, many items in this document have been <u>hyperlinked</u>, including the contents below. By clicking on the hyperlink, you can more easily navigate through the document.

- 1. Addition
- 2. Subtraction
- 3. Multiplication
- 4. Division
- 5. Mathematical Language
- 6. Glossary

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Addition

Objective and Strategies	Concrete	Pictorial	
Combining two parts to make a whole: part- whole model	Use cubes to add two numbers together as a group or in a bar.	3 3	
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer	12 + 5 = 17 $4 + 5 = 17$ $4 + 5 = 17$ $4 + 5 = 17$ $4 + 5 = 17$ $4 + 5 = 17$ $4 + 5 = 17$ $4 + 5 = 17$ $10 + 11 + 12 + 13 + 14 + 15 + 16 + 17 + 18 + 19 + 20$ Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the
Regrouping to make 10.	6 + 5 = 11 Start with the bigger number and use the smaller number to make 10.	Use pictures or a number line. Regroup or partition the smaller number to make 10. 9 + 5 = 14 $9 + 5 = 14$ $1 4$ $+1$ $+1$ $+4$ $+1$ $+4$ $+1$ $+1$ $+4$ $+4$ $+3$ $+4$ $+4$ $+4$ $+4$ $+4$ $+4$ $+4$ $+4$	If I am at s
Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	(4)+ 7 10



Use the part-part whole diagram as shown above to move into the abstract.

Abstract



10= 6 + 4

5 + 12 = 17

ne larger number in your head and count on the smaller number to find your answer.



seven, how many more do I need to make 10. How many more do I add on now?



Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters. T O Image: Comparison of the tens of	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.	$\frac{Calculations}{21 + 42 =}$ $\frac{21}{42}$
Column method- regrouping	Make both numbers on a place value grid. Image: the second seco	Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.	Start by partitioning the numbers before moving on to clearly show the exchange below the addition. $20 + 5 536 40 + 8 + 85 60 + 13 = 73 621 11 As the children move on, introduce decimals with the same numberof decimal places and different. Money can be used here. 72.8 \pm 2 3 . 5 9 \pm 54.6 \pm $

Subtraction

Objective and Strategies	Concrete	Pictorial	
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. 6 - 2 = 4	Cross out drawn objects to show what has been taken away. $ \begin{array}{c} & & & & & & \\ & & & & & & \\ & & & & $	
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13-4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10	Put 13 numb
Find the difference	Compare amounts and objects to find the difference. Use cubes to build towers or make bars to find the difference 12 Use basic bar models with items to find the difference.	Find the difference in age between them. Count on to find the difference. Comparison Bar Models Comparison Bar Models Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 22	Hanna sandw

Abstract

18 -3= 15

8 – 2 = 6

3 in your head, count back 4. What ber are you at? Use your fingers to help.

ah has 23 sandwiches, Helen has 15 viches. Find the difference between the number of sandwiches.

Part Part Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part part whole model.	10 Move to usir
Make 10	14 - 9 = Image: Constrained by the second	13 - 7 = 6 3 4 - 3 4 - 1 2 0 3 14 15 16 17 18 19 20 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	How many d How many d
Column method without regrouping	Tens Ones Image: Ima	Draw the Base 10 or place value counters alongside the written calculation to help to show working. $\begin{array}{c} \hline \\ \hline $	This will lead
Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters	Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.	Children can number into



ng numbers within the part whole model.



836-254=582 u 300 6 130 4 200 50 2 500 80

n start their formal written method by partitioning the o clear place value columns.

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Multiplication

Objective and Strategies Concrete		Pictorial	
	Use practical activities to show how to double a number.	Draw pictures to show how to double a number.	
Doubling	double 4 is 8 $4 \times 2 = 8$	Double 4 is 8	1
Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in mu Write seque
Repeated addition	Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \end{array} $ $ \end{array} $	Write additi
Arrays- showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences.	Draw arrays in different rotations to find commutative multiplication sentences.	Use an array addition.



y to write multiplication sentences and reinforce repeated



	10	8
10	100	80
3	30	24

1000	300	40	2
10000	3000	400	20
8000	2400	320	16

		-						
	Image: Second secon							
	Children can continue to be supported by place value counters at the	Bar modelling and number lines can support learners when solving	Start with lo	ong multiplication, remindi	ng the ch	ildren	abou	t linin
Column multiplication	stage of multiplication.	problems with multiplication alongside the formal written methods. 51 59 59 59 59 59 59 59 59 59 59 59 59 59	If it helps, ch answer. 32 x 24 8 120 40 600 768	hildren can write out what $ \begin{array}{c} (4 \times 2) \\ (4 \times 30) \\ (20 \times 2) \\ (20 \times 30) \end{array} $	they are 	2 2 2 6	g next 7 6 1 1 4 0 6	: to th 4 3 2 0 0 0 2
		250ml) -> 8 = 250ml 16 = 250ml	This moves t	to the more compact metł	nod.			
	It is important at this stage that they always multiply the ones first	4 + 250 ml 4 + 250 ml 4 - 250 ml		2 3	1			
	and note down their answer followed by the tens which they note below.	4 + 4 + 8 + 8 + 16 5 + 8 = 40jug6		134	12			
				x 1	8			
				134	2.0			
				107	20			
				1073	36			
				241	o 6			

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Division

Objective and Strategies	Concrete	Pictorial	
Sharing objects into groups	$\label{eq:harden} \begin{split} & \ensuremath{\mathbb{I}} & \e$	Children use pictures or shapes to share quantities. $ \begin{array}{cccc} & & & & & & & & & & & & & & & & & & &$	Shar
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. 96 ÷ 3 = 32 96 ÷ 3 = 32 90 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	Divide
Division within arrays	$ \begin{array}{c} \label{eq:constraint} \text{Link division to} \\ \text{multiplication by creating an} \\ \text{array and thinking about the} \\ \text{number sentences that can} \\ \text{be created.} \end{array} \\ \\ \text{E.g. } 15 \div 3 = 5 5 \times 3 = 15 15 \div 5 = 3 3 \times 5 = 15 \\ \end{array} $	Image: Constraint of the second se	Find the inve four linking r

e 9 buns between three people.

9 ÷ 3 = 3

28 ÷ 7 = 4

28 into 7 groups. How many are in each group?

erse of multiplication and division sentences by creating number sentences.

7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7

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	14 ÷ 3 =		Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.	Complete wr
Division with a remainder	Divide objects between groups and see I	how much is left over	0 4 8 12 13 Draw dots and group them to divide an amount and clearly show a remainder.	29 ↑ dividend
			() () () () () () () () () ()	
	Tens Units		Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.	Begin with d
	3 2 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	bus stop method <u>Calculations</u> 42 ÷ 3	Encourage them to move towards counting in multiples to divide more efficiently.	Move onto c
Short division				Finally move
	Start with the biggest place value, we are sh groups. We can put 1 ten in each group and	i haring 40 into three we have 1 ten left over. We exchange		
		this ten for ten ones and then share the ones equally among the groups.		
		We look how much in 1 group so the answer is 14.		



Correct Mathematical Language

High expectations of the mathematical language used are essential, with staff only accepting what is correct. Consistency across the school is key:

Correct Terminology	Incorrect Terminology
ones	units
is equal to (is the same as)	equals
zero	oh (the letter o)
exchange	stealing
exchanging	borrowing
regrouping	
calculation	generic term of 'sum' or 'number sentence'
equation	
known	
unknown	
whole	
part	

Definiti
Describes angles betwee
Adjoining (as used to descr
Every other one in
The number of degrees rot
The amount of space within a perime
The arrangement of numbers
A number representing a set of numbers
the numbers by the i
A line dividing a shape into t

Concept	Definitio
Baker's dozen	The colloquial name given
Base	The line or face on which a
Base angles	Those angles adjacent to t
Bisect	To divide into two
Breadth	Breadth is another name for width. It is
	side.

Concept	Definitio
Capacity	The amount of space in an object (the a
Cardinal number	A number that shows qua
Carroll Diagram	A number that shows qua
Circumference	The distance around a cir
Composite number	A number with more t
Congruent	Congruent shapes are the same
Consecutive	Consecutive numbers follow in order w
Coordinates	Numbers used to locate

on

en 0 and 90 degrees.

ribe lines and angles).

a sequence.

tated around a point.

eter (expressed in square units).

from smallest to largest.

s (obtained by dividing the total of numbers itself).

two symmetrical parts.

n

to the number 13.

a shape is standing.

he base of a shape.

equal parts.

the distance across from side to

on

mount of liquid or air it contains). Intity but not order. Intit order. Intity but not o

Concept	Definition
Denominator	The number below the line in a fraction.
Descending order	The arrangement of numbers from the largest to smallest.
Diagonal	A straight line connecting two non- adjacent vertices (corners) of a polygon.
Difference	By how much a number is bigger or smaller than another.
Digit	Any number from 0 to 9 (inclusive).
Digital root	The digital root of 58 is 4 because 5 + 8 = 13 and 1 + 3 = 4
Dimensions	The measurements of a shape (i.e. length, width, height).
Dodecagon	A twelve sided polygon.

Concept	Definitior
Edge	The intersection of two faces of a t
Equation	A statement of equality between two e
Equilateral triangle	A triangle with congruent (equ
Even number	A positive or negative number
Exterior	Outside.

Concept	Definitio
Face	A plane surface of a three-c
Face value	The numeral itself despite its position in a
	in 38,250 is
Factor	A number which will divide exact

Concept	Definitio
Greater than	An inequality between numbers. The sy than is an arrow pointing toward
Gross	The name given to the

three-dimensional object. expressions (e.g. 3 x 4 = 6 + 6). ual) sides and angles. exactly divisible by 2.

dimensional object.

a number (e.g. the face value of 8 8).

tly into another number.

mbol used to represent greater ds the smallest number. number 144.

Concept	Definitio
Hendecagon	A two dimensional shape with eleven side undecago
Heptagon	A two dimensional shape with seven side septagor
Hexagon	A polygon with s
Horizontal	Describes a line or plane paralle

Concept	Definition
Improper fraction	A fraction whose numerator is equal to o
Integer	A negative or positive w
Interior	Inside.
Intersection	The point or line where two line
Irregular shapes	Shapes which do not have all congruent
Isosceles triangle	A triangle which has two equal

Concept	Definition
Kite	A quadrilateral that has two adjacent pairs
	and at least one pair of opposition of a stress of a s

Concept	Definition
Less than	An inequality between numbers. The symbolic an arrow pointing towards the
Lozenge	Another name for a

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es and eleven angles also called an on.

les and seven angles also called a n.

six sides.

el to the earth's surface.

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or greater than it denominator. whole number.

es or two faces meet.

sides and all congruent angles.

sides of equal length.

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s of sides that are equal in length, site angles are equal.

ool used to represent less than is e smallest number. rhombus.

Concept	Definitio
Mean	The average of a set of numbers. The su divided by the total number
Median	The middle value of a set
Mode	The value that occurs the mos
Multiple	The product of a given numbe

Concept	Definitior
Numerator	The number above the li

Concept	Definition
Oblique	Oblique means slopin
Oblong	A shape with two pairs of straight, unequa
	known as a rect
Obtuse angle	An angle between 90 an
Octagon	A polygon with eight sides
Odd number	A number that when divided by two
Ordinal number	Describes a position in a n

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um of the values in a set of data of items in that set. of ordered data. of often in a set of data er with another factor.

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ne in a fraction.

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g or slanting.

al sides and four right angles. Also tangle.

nd 180 degrees.

and eight angles.

leaves a remainder of one.

umber sequence.

Concept	Definitio
Parallel lines	Lines with no common points and alw
Parallelogram	A four-sided polygon with opposite side opposite angles are e
Perimeter	The length of the distance around
Perpendicular line	A line at right angles to and
Polyhedron	A three dimensional shape
Place value	Indicates the position of a numeral (e.g. 30)
Prime number	A number with only two factors, 1 and i 23)
Product	The result when two or more n

Concept	Definition
Quadrant	A quarter of the area of a circle which
Quotient	The result when one number is div
Quindecagon	A polygon with fifteen sides

Concept	Definition
Rectangle	A quadrilateral with opposite sides equal right angle
Reflex angle	An angle greater than
Rhombus	A parallelogram with congruent sides. C opposite sides are ec
Roman numerals	Seven letters are used in combina I = 1 V = 5 X = 10 L = 50 C = 10
Rotational symmetry	A shape is said to have rotational symmetric positions when rotated a
Rounding	An approximation used to express a num

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vays the same distance apart. des equal and parallel and the equal in size.

I the boundary of a shape.

other line or plane.

e with plane faces.

the place value of the 3 in 738 is

itself (e.g. 2,3,5,7,11, 13, 17, 19,

umbers are multiplied.

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h also contains a right angle. vided by another number.

and fifteen angles.

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and parallel and containing four

180 degrees.

Opposite sides are parallel and qual in size.

ation to write numbers:

00 D = 500 M = 1000

ry if it looks the same in different about its centre.

nber in a more convenient way.

Concept	Definitio
Scalene triangle	A triangle that has three sides of differe
Score	The name given to the
Squared	A number squared is a number
Square number	A number whose units can be arr
	1,4,9,16,25,36,4
Sum	The result when two or more num
Symmetrical	A shape is symmetrical if it is identical on e
	two parts

Concept	Definition
Tally	A record of items using vertical and obliq
Tetragon	A four sided sh
Tessellation	Shapes fitted together with a number of e
	or gaps.
Translation	This takes place when a shape is moved fr
	sliding it (without rotating, ref
Trapezium	A quadrilateral with two
Triangular number	A number whose units can be arranged ir
	21)
Trigon	A three sided s

Concept	Definition
Vertex	The point at which two or more line segm polyhedron m
Vertical line	A line which is at right angles

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ent length and no equal angles. e number 20.

er multiplied by itself.

ranged into a square (e.g. 49,64...)

nbers are added together.

either side of a line dividing it into s.

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ue lines to represent each item.

hape.

exact copies and with no overlaps

rom one place to another just by flecting or enlarging).

parallel sides.

nto a triangle (e.g. 1, 3, 6, 10, 15,

shape.

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nents or two or more edges of a neet.

to a horizontal line.